

## Supporting Information

### Electron Binding Energy Spectra of $\text{Al}_n\text{Mo}^-$ Clusters: Measurements, Calculations and Theoretical Analysis

Paulo H. Acioli<sup>1</sup>, Xinxing Zhang<sup>2</sup>, Kit H. Bowen Jr.<sup>3\*</sup> and Julius Jellinek<sup>4\*</sup>

<sup>1</sup>Department of Physics, Northeastern Illinois University, Chicago, Illinois 60625, USA

<sup>2</sup>Collaborative Innovation Center of Chemical Sciences and Engineering, College of Chemistry, Nankai University, Tianjin 300071, China

<sup>3</sup>Departments of Chemistry and Materials Science, Johns Hopkins University, Baltimore, Maryland 21218, USA

<sup>4</sup>Chemical Sciences and Engineering Division, Argonne National Laboratory, Argonne, Illinois 60349, USA

## 1. Results of tests

**Table S1.** Calculated DFT (BPW91, PBE and BP86) and measured (Exp) results for Mo, Mo<sub>2</sub>, Al, and Al<sub>2</sub>. IP, IP<sub>a</sub>, EA and r<sub>e</sub> denote ionization potential, adiabatic ionization potential, electron affinity and interatomic equilibrium distance, respectively.

System	Property	BPW91	PBE	BP86	Exp
Mo	IP(eV)	7.604	7.573	7.731	7.0924 <sup>1</sup>
	EA(eV)	0.355	0.496	0.722	0.7473 <sup>2</sup>
Mo <sub>2</sub>	BE(eV/atom)	1.415	1.643	1.789	2.24 <sup>3</sup>
	IP <sub>a</sub> (eV)	7.122	7.166	7.324	6.95 <sup>3</sup>
	EA(eV)	0.753	0.762	0.904	> 1.0 <sup>4</sup>
	r <sub>e</sub> (Å)	1.984	1.983	1.985	1.94 <sup>3</sup>
Al	IP (eV)	6.060	6.169	6.243	5.984 <sup>5</sup>
	EA(eV)	0.280	0.270	0.335	0.441 <sup>6</sup>
Al <sub>2</sub>	BE(eV/atom)	0.677	0.723	0.673	0.67 <sup>7</sup>
	IP <sub>a</sub> (eV)	6.014	5.922	5.941	5.989 <sup>8</sup>
	EA(eV)	1.467	1.469	1.540	1.46 <sup>9</sup>
	r <sub>e</sub> (Å)	2.571	2.571	2.580	2.701 <sup>7</sup>

<sup>1</sup> Rayner, D. M.; Mitchell, S. A.; Bourne, O. L.; Hackett, P. A. First-Ionization Potential of Niobium and Molybdenum by Double-Resonance, Field-Ionization Spectroscopy. *J. Opt. Soc. Am. B* **1987**, *4*, 900-905.

<sup>2</sup> Bilodeau, R. C.; Scheer, M.; Haugen, H. K. Infrared Laser Photodetachment of Transition Metal Negative Ions: Studies on Cr<sup>-</sup>, Mo<sup>-</sup>, Cu<sup>-</sup> and Ag<sup>-</sup>. *J. Physics B: Atom. Mol. Opt. Phys.* **1998**, *31*, 3885-3892.

<sup>3</sup> Simard, B.; Lebeault-Dorget, M.; Marijnissen, A.; ter Meulen, J. J. Photoionization Spectroscopy of Dichromium and Dimolybdenum: Ionization Potentials and Bond Energies. *J. Chem. Phys.* **1998**, *108*, 9668-9674.

<sup>4</sup> Balasubramanian, K. Spectroscopic Properties of Mo<sub>2</sub><sup>-</sup> and Mo<sub>2</sub><sup>+</sup>. *Chem. Phys. Lett.* **2002**, *365*, 413-420.

<sup>5</sup> Moore, C. E. Atomic Energy Levels and Other Spectroscopic Data - NIST Page. *Natl. Bur. Stand. Circ.* 467, US GPO, Washington, D.C., 1949, 1952.

<sup>6</sup> Hotop H.; Lineberger, W. C. Binding Energies in Atomic Negative Ions: II. *J. Phys. Chem. Ref. Data* **1985**, *14*, 731-750.

<sup>7</sup> Fu, Z.; Lemire, G. W.; Bishea, G. A.; Morse, M. D. Spectroscopy and Electronic Structure of Jet-Cooled Al<sub>2</sub>. *J. Chem. Phys.* **1990**, *93*, 8420-8441.

- <sup>8</sup> Harrington J. E.; Weisshaar, J. C. Adiabatic Ionization Potential of Al<sub>2</sub> and Vibrational Spectrum of the  $X^2\Sigma_g^+$  State of Al<sub>2</sub><sup>+</sup>. *J. Chem. Phys.* **1990**, *93*, 854-855.
- <sup>9</sup> Li, X.; Wu, H.; Wang, X.-B.; Wang, L.-S. *s-p* Hybridization and Electron Shell Structures in Aluminum Clusters: A Photoelectron Spectroscopy Study. *Phys. Rev. Lett.* **1998**, *81*, 1909-1912.

The comparison of the calculated and measured results, especially those for electron affinities, points to BP86 as the optimal choice for the exchange-correlation functional.

## 2. Results of calculations for the lowest energy structures of Al<sub>n</sub>Mo<sup>-</sup>, n=3-5 and 7, the Mo and Al atoms, and the lowest energy structures of Al<sub>n</sub><sup>-</sup>, n=4 and 5.

**Table S2.** Negatives of the upper Kohn-Sham (KS) eigenenergies ( $-\varepsilon_i$ ) and their corresponding correction terms ( $\Delta_i$ )<sup>10</sup> and electron binding energies ( $EBE_i$ ) for the lowest energy (C<sub>3v</sub>) structure of the Al<sub>3</sub>Mo<sup>-</sup> cluster. All values are in eV. Bold numbers/letters indicate the part of the calculated spectrum whose  $EBE_i$  fall under the measured EBE spectrum.

Cluster	<i>i</i>	Eigenstate label and occupancy	$-\varepsilon_i$	$\Delta_i$	$EBE_i$
Al <sub>3</sub> Mo <sup>-</sup>	<b>1</b>	<b>e<sup>2</sup>(β)</b>	<b>0.249</b>	<b>1.980</b>	<b>2.229</b>
	<b>2</b>	<b>a<sub>1</sub><sup>1</sup>(α)</b>	<b>0.345</b>	<b>1.986</b>	<b>2.331</b>
	<b>3</b>	<b>e<sup>2</sup>(α)</b>	<b>0.586</b>	<b>2.000</b>	<b>2.586</b>
	<b>4</b>	<b>e<sup>2</sup>(α)</b>	<b>0.707</b>	<b>2.008</b>	<b>2.714</b>
	<b>5</b>	<b>a<sub>1</sub><sup>1</sup>(α)</b>	<b>0.757</b>	<b>2.011</b>	<b>2.768</b>
	<b>6</b>	<b>a<sub>1</sub><sup>1</sup>(β)</b>	<b>0.847</b>	<b>2.016</b>	<b>2.862</b>
	<b>7</b>	<b>a<sub>1</sub><sup>1</sup>(α)</b>	<b>1.216</b>	<b>2.034</b>	<b>3.250</b>
	8	a <sub>1</sub> <sup>1</sup> (β)	3.232	2.137	5.370

<sup>10</sup> Jellinek, J.; Acioli, P. H. Converting Kohn-Sham Eigenenergies into Electron Binding Energies. *J. Chem. Phys.* **2003**, *118*, 7783-7796.

The listed  $EBE_i$  values calculated with the orbital-specific corrections  $\Delta_i$  are used in the main text.

**Table S3.** The same as Table S2, but for the lowest energy ( $C_{2v}$ ) structure of the  $Al_4Mo^-$  cluster.

Cluster	$i$	Eigenstate label and occupancy	$-\varepsilon_i$	$\Delta_i$	$EBE_i$	$EBE_i$ (constant correction)
$Al_4Mo^-$	1	$b_1^1(\beta)$	<b>0.246</b>	<b>1.885</b>	<b>2.131</b>	<b>2.131</b>
	2	$b_1^1(\alpha)$	<b>0.514</b>	<b>1.891</b>	<b>2.405</b>	<b>2.399</b>
	3	$a_1^1(\alpha)$	<b>0.536</b>	<b>1.892</b>	<b>2.428</b>	<b>2.421</b>
	4	$b_2^1(\beta)$	<b>0.655</b>	<b>1.895</b>	<b>2.549</b>	<b>2.540</b>
	5	$a_1^1(\beta)$	<b>0.717</b>	<b>1.896</b>	<b>2.613</b>	<b>2.602</b>
	6	$b_2^1(\alpha)$	<b>0.812</b>	<b>1.899</b>	<b>2.711</b>	<b>2.697</b>
	7	$a_1^1(\alpha)$	<b>0.912</b>	<b>1.901</b>	<b>2.813</b>	<b>2.797</b>
	8	$a_1^1(\beta)$	<b>1.391</b>	<b>1.915</b>	<b>3.306</b>	<b>3.276</b>
	9	$a_2^1(\beta)$	<b>1.516</b>	<b>1.918</b>	<b>3.435</b>	<b>3.401</b>
	10	$a_1(\alpha)$	1.585	1.920	3.506	3.470
	11	$a_2(\alpha)$	1.601	1.921	3.522	3.486
	12	$a_1(\beta)$	2.700	1.956	4.656	4.585
	13	$a_1(\alpha)$	2.963	1.965	4.928	4.848

The  $EBE_i$  values calculated with the constant correction  $\Delta_i$  (correction for the HOMO KS eigenenergy) and listed in the last column of the table are used in the main text.

**Table S4.** The same as Table S2, but for the lowest energy ( $C_{4v}$ ) structure of the  $Al_5Mo^-$  cluster.

Cluster	$i$	Eigenstate label and occupancy	$-\varepsilon_i$	$\Delta_i$	$EBE_i$	$EBE_i$ (constant correction)
$Al_5Mo^-$	1	$a_1^2$	<b>0.269</b>	<b>1.895</b>	<b>2.163</b>	<b>2.163</b>
	2	$b_2^2$	<b>0.743</b>	<b>1.900</b>	<b>2.643</b>	<b>2.638</b>
	3	$a_1^2$	<b>0.978</b>	<b>1.902</b>	<b>2.880</b>	<b>2.873</b>
	4	$e^4$	<b>1.345</b>	<b>1.905</b>	<b>3.250</b>	<b>3.239</b>
	5	$b_1^2$	1.898	1.909	3.807	3.792
	6	$a_1^2$	3.721	1.920	5.641	5.616

The  $EBE_i$  values calculated with the constant correction  $\Delta_i$  (correction for the HOMO KS eigenenergy) and listed in the last column of the table are used in the main text.

**Table S5.** The same as Table S2, but for the lowest energy ( $C_{2v}$ ) structure of the  $Al_7Mo^-$  cluster.

Cluster	$i$	Eigenstate label and occupancy	$-\varepsilon_i$	$\Delta_i$	$EBE_i$	$EBE_i$ (constant correction)
$Al_7Mo^-$	1	$a_2^2$	<b>0.894</b>	<b>1.750</b>	<b>2.644</b>	<b>2.644</b>
	2	$b_1^2$	<b>1.109</b>	<b>1.753</b>	<b>2.862</b>	<b>2.859</b>
	3	$a_1^2$	<b>1.376</b>	<b>1.756</b>	<b>3.132</b>	<b>3.126</b>
	4	$a_1^2$	<b>1.377</b>	<b>1.756</b>	<b>3.133</b>	<b>3.127</b>
	5	$b_1^2$	<b>1.484</b>	<b>1.758</b>	<b>3.242</b>	<b>3.234</b>
	6	$b_2^2$	1.811	1.762	3.573	3.561
	7	$a_1^2$	1.960	1.765	3.724	3.710
	8	$a_1^2$	3.232	1.787	5.019	4.982

The  $EBE_i$  values calculated with the constant correction  $\Delta_i$  (correction for the HOMO KS eigenenergy) and listed in the last column of the table are used in the main text.

**Table S6.** The same as Table S2, but for the Mo atom.

Atom	$i$	Eigenstate label and occupancy	$-\varepsilon_i$	$\Delta_i$	$EBE_i$
Mo	1	$4d^5(\alpha)$	4.628	3.103	7.731
	2	$5s^1(\alpha)$	4.858	3.167	8.026

The listed  $EBE_i$  values calculated with the orbital-specific corrections  $\Delta_i$  are used in the main text.

**Table S7.** The same as Table S2, but for the Al atom.

Atom	$i$	Eigenstate label and occupancy	$-\varepsilon_i$	$\Delta_i$	$EBE_i$
Al	1	$3p^1(\alpha)$	3.093	3.150	6.243
	2	$3s^1(\beta)$	7.514	3.363	10.664
	3	$3s^1(\alpha)$	8.074	3.390	11.224

The listed  $EBE_i$  values calculated with the orbital-specific corrections  $\Delta_i$  are used in the main text.

**Table S8.** The same as Table S2, but for the lowest energy ( $D_{2h}$ ) structure of the  $Al_4^-$  cluster.

Cluster	$i$	Eigenstate label and occupancy	$-\varepsilon_i$	$\Delta_i$	$EBE_i$
$Al_4^-$	<b>1</b>	<b><math>b_{3g}^1(\beta)</math></b>	<b>0.214</b>	<b>2.022</b>	<b>2.236</b>
	<b>2</b>	<b><math>b_{3u}^1(\beta)</math></b>	<b>0.253</b>	<b>2.025</b>	<b>2.278</b>
	<b>3</b>	<b><math>b_{3u}^1(\alpha)</math></b>	<b>0.285</b>	<b>2.027</b>	<b>2.312</b>
	<b>4</b>	<b><math>b_{3g}^1(\alpha)</math></b>	<b>0.339</b>	<b>2.030</b>	<b>2.369</b>
	<b>5</b>	<b><math>a_g^1(\alpha)</math></b>	<b>1.296</b>	<b>2.084</b>	<b>3.380</b>
	6	$a_g^1(\beta)$	1.533	2.095	3.628
	7	$b_{2u}^1(\beta)$	3.435	2.179	5.614
	8	$b_{2u}^1(\alpha)$	3.735	2.187	5.922

The listed  $EBE_i$  values calculated with the orbital-specific corrections  $\Delta_i$  are used in the main text.

**Table S9.** The same as Table S2, but for the lowest energy ( $C_s$ ) structure of the  $Al_5^-$  cluster.

Cluster	$i$	Eigenstate label and occupancy	$-\varepsilon_i$	$\Delta_i$	$EBE_i$	$EBE_i$ (constant correction)
$Al_5^-$	<b>1</b>	<b><math>A'^2</math></b>	<b>0.459</b>	<b>1.830</b>	<b>2.289</b>	<b>2.289</b>
	<b>2</b>	<b><math>A'^2</math></b>	<b>0.817</b>	<b>1.840</b>	<b>2.657</b>	<b>2.647</b>
	<b>3</b>	<b><math>A''^2</math></b>	<b>0.912</b>	<b>1.842</b>	<b>2.754</b>	<b>2.742</b>
	4	$A'^2$	2.028	1.873	3.901	3.858
	5	$A'^2$	2.977	1.900	4.877	4.807
	6	$A'^2$	4.376	1.941	6.316	6.206
	7	$A'$	5.423	1.970	7.393	7.253

The  $EBE_i$  values calculated with the constant correction  $\Delta_i$  (correction for the HOMO KS eigenenergy) and listed in the last column of the table are used in the main text.

### 3. Normal mode frequencies, harmonic zero-point energies, and room-temperature thermal energies.

**Table S10.** Normal mode frequencies  $\nu_i$  (in  $\text{cm}^{-1}$ ) for the lowest energy structures of  $\text{Al}_n\text{Mo}^-$ ,  $n=3,4,5$  and 7, the  $C_{4v}$  transition state (TS) configuration of  $\text{Al}_4\text{Mo}^-$ , and the  $C_{2v}$  TS configuration of  $\text{Al}_5^-$ .

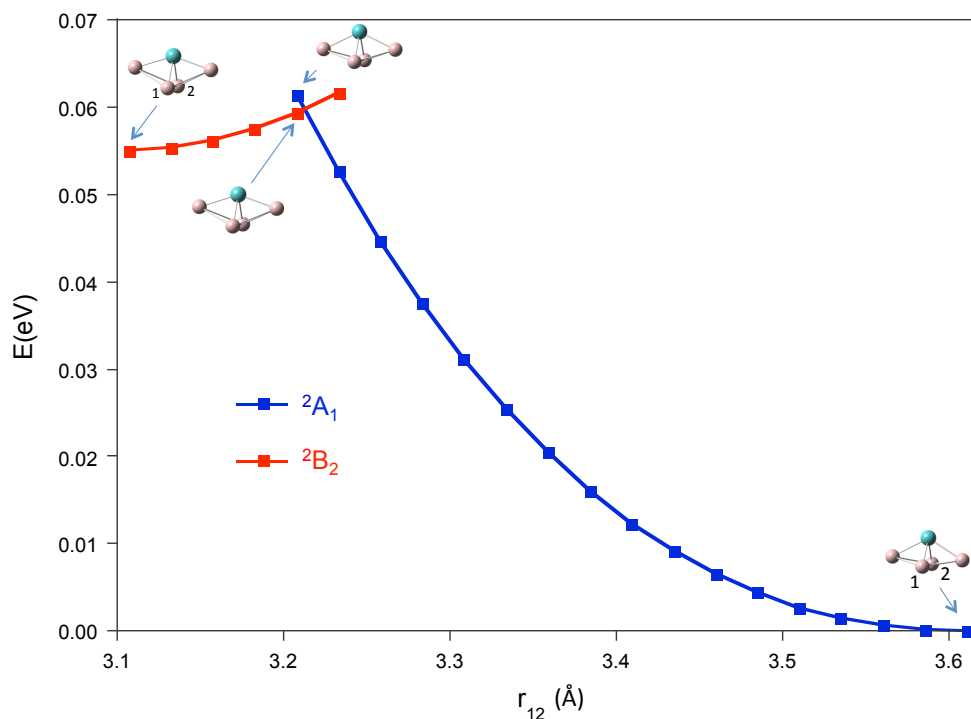
$i$	$\text{Al}_3\text{Mo}^-$	$\text{Al}_4\text{Mo}^-$	$\text{Al}_5\text{Mo}^-$	$\text{Al}_7\text{Mo}^-$	$\text{Al}_4\text{Mo}^-(\text{TS})$	$\text{Al}_5^-(\text{TS})$
	$\nu_i$					
1	142.51	48.87	47.28	74.37	35.35 <i>i</i>	28.93 <i>i</i>
2	142.51	151.79	47.28	101.26	149.53	36.45
3	170.63	156.53	85.71	115.55	178.86	109.11
4	298.95	171.73	97.84	137.07	178.86	155.74
5	298.95	187.27	143.39	152.53	216.01	221.92
6	343.38	253.60	143.39	165.49	246.65	227.48
7		297.54	151.16	166.25	308.96	283.27
8		327.92	261.63	197.19	308.96	339.20
9		344.90	285.00	206.41	338.10	351.83
10			330.26	222.55		
11			330.26	226.91		
12			334.84	233.96		
13				235.10		
14				244.08		
15				266.72		
16				309.27		
17				316.85		
18				358.35		

**Table S11.** Harmonic zero-point energies  $E_0 = 0.5h \sum_i \nu_i$  and room-temperature ( $T=300$  K) thermal vibrational energies  $E_T = fkT$  (all in eV) for the lowest energy structures of  $\text{Al}_n\text{Mo}^-$ ,  $n=3,4,5$  and 7, the  $C_{4v}$  TS configuration of  $\text{Al}_4\text{Mo}^-$ , and the  $C_{2v}$  TS configuration of  $\text{Al}_5^-$ .  $h$  is Planck's constant,  $f$  is the number of vibrational modes with real-valued frequencies, and  $k$  is Boltzmann's constant.

	$\text{Al}_3\text{Mo}^-$	$\text{Al}_4\text{Mo}^-$	$\text{Al}_5\text{Mo}^-$	$\text{Al}_7\text{Mo}^-$	$\text{Al}_4\text{Mo}^-(\text{TS})$	$\text{Al}_5^-(\text{TS})$
$E_0$	0.087	0.120	0.140	0.231	0.119	0.107
$E_T$	0.155	0.232	0.310	0.465	0.207	0.207



#### 4. Crossing of two electronic states of the $\text{Al}_4\text{Mo}^-$ cluster.



**Figure S1.** Crossing of the  $^2A_1$  and  $^2B_2$  electronic states corresponding to two  $C_{2v}$  forms of the  $\text{Al}_4\text{Mo}^-$  cluster (see the main text for details).

The two graphs were obtained through constrained energy minimizations on grids of  $r_{12}$  distances (distances between atoms 1 and 2) starting from the corresponding equilibrium structures represented by the bottoms of the two graphs. Near the crossing point the constrained minimizations also involved fixing the corresponding electronic states. The energy at the crossing point ( $r_{12}=3.21$  Å) obtained through interpolation is just 0.060 eV above the equilibrium energy of the most stable form of the cluster.